

Sections 5.5 Multiplying and Dividing a Polynomial by a Constant

Remember the signs:

| | |
|------------------|------------------|
| $+ \times + = +$ | $- \times + = -$ |
| $- \times - = +$ | $+ \times - = -$ |

When multiplying or dividing.....

| | |
|----------------|----------------|
| $+ \div + = +$ | $- \div + = -$ |
| $- \div - = +$ | $+ \div - = -$ |

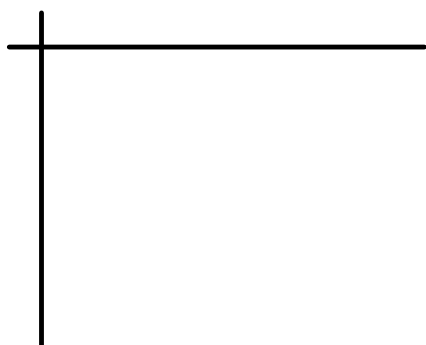
You will be expected to multiply and divide polynomials:

- using algebra tiles
- using area model
- symbolically

Example 1 Multiplying a polynomial by a constant.

(a) $3(2x)$

Use Algebra Tiles:



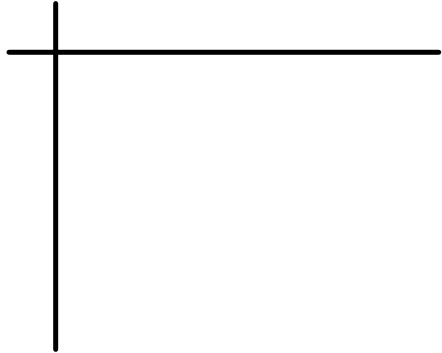
Use Algebra:

Use an Area Model:

Think: $A = L \times W$
Area of a rectangle

(b) $3(2x + 2)$

Use Algebra Tiles:



Use an Area Model:

Use Algebra:

Multiply each term of the polynomial inside the bracket by the monomial in front of the bracket.

Example 2 Multiply using algebra tiles.

(a) $2(2x + 3)$

(b) $4(2x + 1)$

Example 3 How would you sketch **negatives** with algebra tiles?

(a) $3(-2m + 4)$

(b) $-4(x + 2)$

Your Turn Multiply using algebra tiles. Check your answer using algebra

(c) $-(2x - 1)$

Example 4 Multiply using distributive property using algebra.
Be careful with signs!

(a) $3(-2m + 4)$

(b) $-8(x - 5)$

(c) $-2(-n^2 + 2n - 1)$

(d) $-4(x + 2)$

Your Turn Multiply using the distributive property.

(e) $3(x - 7)$

(f) $-10(x + 2)$

(g) $3(-8 - 7x)$

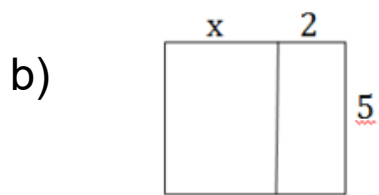
(h) $2(x + 10)$

Example 5 Sketch the answer using the area model.

$$-2(-n^2 + 2n - 1)$$

Example 6 Determine the length, width and area of the following.
Write a multiplication sentence.





Example 7 Determine the area of the following. Write a multiplication sentence.

a) Length = $2x + 2$
Width = 4

b) Length = $-x + 3$
Width = 2

When dividing by a constant term → think about arranging the tiles into equal groups.

Example 8 Divide a polynomial by a constant. Use algebra tiles.

(a) $\frac{4x^2}{2}$

(b) $\frac{4x^2 - 8x}{2}$

Example 9 Divide symbolically.

a). $\frac{4x^2}{2}$

Divide the numbers.
Reduce to lowest terms if possible.

b). $\frac{4x^2 - 8x}{2}$

Rewrite as two fractions.
Divide both monomials.

NOTE:

However many terms are in the numerator, that's how many terms are in your answer. When dividing a trinomial by a monomial, you will have a trinomial answer.

Example 10 Divide

Be careful when dividing by negatives!

(a)
$$\frac{12m^2 + 6m - 9}{3}$$

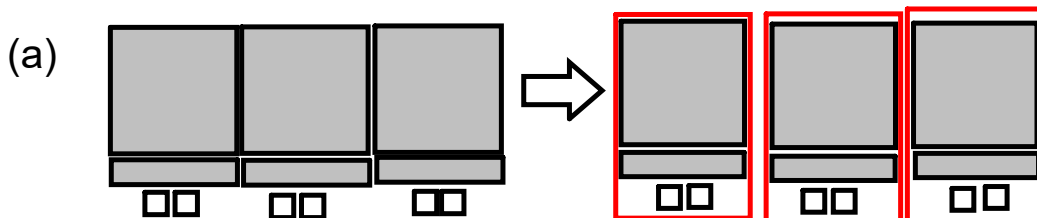
(b)
$$\frac{-3y^2 + 15xy - 21x^2}{-3}$$

Your Turn

(c)
$$\frac{24m^2}{8}$$

(d)
$$\frac{-6p^2 + 9p - 3}{-3}$$

Example 11 Write a division sentence to represent each diagram below?



(b) 5 Area = $15x^2 - 10x + 20$ $?$

Example 12

(a) The perimeter of a square is $16x^2 - 12y$. What is the length of each side of the square?

(b) If the area of a rectangle is $21y^2 + 14y - 7$ and the width is 7cm, what is the length of the rectangle?

| Work Book Questions | Extra Practice Questions |
|--|--|
| p.246 - 248 #3cd, 8a(i)(ii)(iii)(iv), 9ab, 11ab, 12, 13bdf, 14, 15abcdef, 16aceg, 17abc, 18a(i)(ii)(iii)(iv)(v)(vi), 20ab, 21ab, 22ace, 23ac | p.246-248 #5, 6, 7, 10, 11cdef, 13ace, 16bdfh, 17def, 22bd, 23bd |